This paper introduces a new comprehensive panel of annual state-level income inequality measures spanning the postwar period 1945–2004. For many states, the share of income held by the top decile experienced a prolonged period of stability after World War II, followed by a substantial increase in inequality during the 1980s and 1990s. This paper also presents an examination of the long-run relationship between income inequality and economic growth. Our findings indicate that the long-run relationship between inequality and growth is positive in nature and driven principally by the concentration of income in the upper end of the income distribution. (JEL D31, O40)

I. INTRODUCTION

Rising income inequality in the United States over the past quarter century is well documented (see, e.g., Gottschalk 1997; Krueger 2003; Levy and Murnane 1992; Piketty and Saez 2003). Whether and by how much this change in inequality is associated with a change in economic performance is an important question, yet recent empirical work has been largely inconclusive. Positive relationships between income inequality and economic growth have been found by Partridge (1997, 2005) using a panel of states and by Forbes (2000) using a panel of countries. Empirical work by Panizza (2002) and Quah (2001), however, has found little or no stable relationship between inequality and growth; the results appear to be extremely sensitive to the econometric specification. Additionally, Barro (2000) has found evidence that the relationship is nonlinear, with inequality being positively related to growth among wealthier countries like the United States but negatively related to growth among low-income countries.

Much of this recent empirical literature was initiated by the important work of Deininger and Squire (1996), who constructed a large cross-national panel of inequality measures containing several time-series observations for each nation spaced over multiple decades. A parallel empirical literature also emerged using U.S. state-level data, with income inequality measures typically spaced at 10-yr intervals (see, e.g., Panizza 2002; Partridge 1997, 2005). Both the state-level and the cross-national empirical literatures benefited by exploiting the more advanced panel data econometrics afforded by the large-N, small-T panel dimensions.

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ABBREVIATIONS

ARDL: Autoregressive Distributive Lag
BEA: Bureau of Economic Analysis
CPS: Current Population Survey
FE: Fixed Effects
IRS: Internal Revenue Service
MG: Mean Group
NBER: National Bureau of Economic Research
SBC: Schwarz Bayesian Criterion
In this paper, we offer a new, more comprehensive panel of state-level income inequality measures and use this panel to reevaluate the empirical inequality-growth relationship. This panel has the unique feature of being large in both $N$ and $T$, with annual observations of the 48 contiguous states for the entirety of the postwar period 1945–2004. For nearly all the states in the panel, the share of income held by the top decile experienced a prolonged period of stability after World War II, followed by a substantial increase during the 1980s and 1990s. These state-level trends appear to closely replicate the overall trends in aggregate U.S. inequality found by Piketty and Saez (2003).

Exploiting the large and balanced size of our inequality panel, we explore the long-run relationship between inequality and growth via three alternative dynamic panel error-correction estimators: the fixed effects (FE) estimator, the mean group (MG) estimator of Pesaran and Smith (1995), and the pooled MG estimator of Pesaran, Shin, and Smith (1999). The greater homogeneity of state-level data helps mitigate the difficulty in adequately capturing structural differences across international panels of earlier studies such as Forbes (2000) and Barro (2000). Corruption levels, labor market flexibility, tax neutrality, tradition of entrepreneurship, and many other factors are only poorly measured, if at all (Barro 2000, 10–11), and these sources of heterogeneity are much more likely to contribute to omitted variable bias across countries than across states. The results from our analysis indicate that the long-run relationship between the top decile share of income and economic growth is positive in nature. Moreover, an evaluation of several alternative income inequality measures suggests that this positive relationship is driven primarily by the concentration of income in the upper end of the income distribution.

The structure of the paper is as follows. Section II presents the new panel of annual state-level inequality measures and includes an important discussion of its key limitations. Section III then offers an empirical investigation on the impact of income inequality on the growth rate of real income per capita. Finally, Section IV offers a brief set of conclusions.

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1. This new panel of annual state-level income inequality measures may be obtained online at http://www.shsu.edu/~eco_mwf/inequality.html.

2. The IRS does not, however, provide a meaningful separation of these income sources for each income group at the state-level. Hence, unlike Piketty and Saez (2003), we will be unable to assess the relative impact from changes in each income source (wages and salaries, capital, or entrepreneurial) on income inequality.
After three decades of post–World War II stability, large increases in inequality began in the 1980s, with a significant part of this increase occurring after the Tax Reform Act of 1986, and continued throughout the 1990s (see also Gottschalk 1997; Krueger 2003; Levy and Murnane 1992).

TABLE 1
Descriptive Statistics of the Variables (2004 = 100)

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean</th>
<th>Standard Deviation</th>
<th>Minimum Annual Mean (Year)</th>
<th>Maximum Annual Mean (Year)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Top decile share of income</td>
<td>0.336</td>
<td>0.046</td>
<td>0.282 (1956)</td>
<td>0.430 (2000)</td>
</tr>
<tr>
<td>Top 1% share of income</td>
<td>0.096</td>
<td>0.036</td>
<td>0.047 (1974)</td>
<td>0.172 (2000)</td>
</tr>
<tr>
<td>Gini coefficient</td>
<td>0.493</td>
<td>0.062</td>
<td>0.408 (1956)</td>
<td>0.631 (2004)</td>
</tr>
<tr>
<td>Atkinson index, ( \varepsilon = 0.5 )</td>
<td>0.197</td>
<td>0.037</td>
<td>0.156 (1953)</td>
<td>0.280 (2000)</td>
</tr>
<tr>
<td>Atkinson index, ( \varepsilon = 1.5 )</td>
<td>0.514</td>
<td>0.054</td>
<td>0.429 (1947)</td>
<td>0.618 (2000)</td>
</tr>
<tr>
<td>Theil entropy index</td>
<td>0.478</td>
<td>0.145</td>
<td>0.346 (1953)</td>
<td>0.760 (2000)</td>
</tr>
<tr>
<td>High school attainment</td>
<td>0.351</td>
<td>0.142</td>
<td>0.095 (1945)</td>
<td>0.564 (2004)</td>
</tr>
<tr>
<td>College attainment</td>
<td>0.084</td>
<td>0.051</td>
<td>0.029 (1945)</td>
<td>0.175 (2004)</td>
</tr>
<tr>
<td>Farming ((\times 1,000))</td>
<td>386.4</td>
<td>537.3</td>
<td>285.5 (1987)</td>
<td>511.0 (1946)</td>
</tr>
<tr>
<td>Agriculture services ((\times 1,000))</td>
<td>239.2</td>
<td>505.3</td>
<td>45.5 (1945)</td>
<td>689.7 (2000)</td>
</tr>
<tr>
<td>Mining ((\times 1,000))</td>
<td>694.9</td>
<td>1,444.4</td>
<td>475.1 (1945)</td>
<td>1,275.6 (1971)</td>
</tr>
<tr>
<td>Construction ((\times 1,000))</td>
<td>3,228.5</td>
<td>4,088.1</td>
<td>640.6 (1945)</td>
<td>6,031.4 (2004)</td>
</tr>
<tr>
<td>Manufacturing ((\times 1,000))</td>
<td>14,450.2</td>
<td>17,822.3</td>
<td>7,354.5 (1946)</td>
<td>18,920.0 (2000)</td>
</tr>
<tr>
<td>Transportation ((\times 1,000))</td>
<td>4,153.3</td>
<td>5,136.1</td>
<td>2,166.0 (1947)</td>
<td>7,047.8 (2000)</td>
</tr>
<tr>
<td>Trade ((\times 1,000))</td>
<td>9,723.8</td>
<td>12,733.1</td>
<td>3,178.6 (1945)</td>
<td>17,671.8 (2000)</td>
</tr>
<tr>
<td>Finance, Insurance, and Real Estate ((\times 1,000))</td>
<td>4,019.0</td>
<td>8,095.8</td>
<td>708.9 (1945)</td>
<td>10,385.6 (2004)</td>
</tr>
<tr>
<td>Services ((\times 1,000))</td>
<td>11,946.0</td>
<td>21,644.3</td>
<td>1,885.3 (1945)</td>
<td>37,100.6 (2004)</td>
</tr>
<tr>
<td>Government ((\times 1,000))</td>
<td>10,550.8</td>
<td>13,865.8</td>
<td>2,722.4 (1947)</td>
<td>18,682.3 (2004)</td>
</tr>
</tbody>
</table>

(see also Goldin and Margo 1992). After three decades of post–World War II stability, large increases in inequality began in the 1980s, with a significant part of this increase occurring after the Tax Reform Act of 1986, and continued throughout the 1990s (see also Gottschalk 1997; Krueger 2003; Levy and Murnane 1992).

FIGURE 1
Trends in U.S. Real Income Per Capita and Income Inequality, 1945–2004
The new state-level inequality panel we present appears quite consistent with the aggregate U.S. data of Piketty and Saez. Comparing our measure of the top 10% share of income averaged across the 48 states (shown in Figure 1) to the total U.S. share presented in Piketty and Saez (2003, 11), the mean share of income for the period of commonality (1945–1998) is 32.7% in our panel and 34.0% in the time-series data of Piketty and Saez. The minimum annual share of income is 28.2% in our sample and 31.4% in Piketty and Saez (both occurring in 1953), while the maximum annual share is 41.9% in our panel and 41.4% in Piketty and Saez (both occurring in 1998). Moreover, the Pearson’s correlation coefficient between the two series is 0.980, while the Theil $U$ statistic is 0.044.3

The distinguishing feature of our panel is the construction of annual inequality measures for each of the states. State-level inequality panels have been used before, notably by Panizza (2002) and Partridge (1997, 2005), though these panels are spaced at 10-yr or longer intervals. Figure 2 shows the individual state-level trends in the top 10% share of income and the log of real income per capita. Overall, many of the individual states appear to replicate the general trend and level of U.S. inequality discussed above. The lowest level of income inequality over the 60-yr period occurred in West Virginia (with an average top decile share of income of 30.5%), while the largest level of inequality occurred in Florida and New York (37.7% and 37.5%, respectively). The largest state outlier is Delaware, with a Pearson’s correlation to the top decile share from Piketty and Saez (2003) of only 0.11. The remaining 47 states are highly correlated to the Piketty and Saez data, with Oklahoma having the next-lowest correlation at 0.89.

One significant limitation of IRS income data, however, is the omission of some individuals earning less than a threshold level of gross income. This threshold varies by age and marital status, as well as the tax filing year. For this reason, we follow Piketty and Saez (2003) in using the top decile share of income as our primary measure of inequality.4 Other non-IRS data sources have the clear advantage of not omitting these low-income individuals, but these sources are either not available annually, such as the decennial Census, or, in the case of the March Current Population Survey (CPS), only available annually for more recent years. Akhand and Liu (2002), moreover, provide evidence that these survey-based alternatives suffer additional bias resulting from an “over-reporting of earnings by individuals in the lower tail of the income distribution and under-reporting by individuals in the upper tail of the income distribution” (258). The IRS, unlike the March CPS or Bureau of the Census, will penalize respondents for income reporting errors.

### III. The Relationship Between Income Inequality and Economic Growth

This section explores the relationship between income inequality and economic growth using a methodology that fully exploits the unusually large and balanced size of our panel. We begin with the common autoregressive distributive lag (ARDL) $(p, q, \ldots, q)$ dynamic panel specification:

\[
\Delta y_{i,t} = \sum_{j=1}^{p} \alpha_{ij}y_{i,t-j} + \sum_{j=0}^{q} \beta'_{ij}X_{i,t-j} + \mu_{i} + \tau_{t} + \epsilon_{i,t},
\]

where the number of states $i = 1, 2, \ldots, N$, the number of time periods $t = 1, 2, \ldots, T$, $y_{i,t}$ is the log of real income per capita, $X_{i,t}$ is a vector of explanatory variables that includes a measure of income inequality, $\mu_{i}$ is the time-invariant fixed effect for state $i$, $\tau_{t}$ is the state-invariant time effect for time $t$, and $\epsilon$ is the idiosyncratic, time- and state-varying error term. Adding $y_{i,t-1}$ to each side of Equation (1) yields

\[
y_{i,t} = \sum_{j=1}^{p} \lambda_{ij}y_{i,t-j} + \sum_{j=0}^{q} \beta'_{ij}X_{i,t-j} + \mu_{i} + \tau_{t} + \epsilon_{i,t},
\]

3. The Theil $U$ statistic varies between 0 and 1 and is analogous to an $R^2$ measure, though large values indicate poor performance.

4. Additionally, Reynolds (2006, 2007) has argued that the IRS-based income share measure for the top 1% reported in Piketty and Saez (2003) is seriously flawed, an assessment strongly disputed by Piketty and Saez (2006).
FIGURE 2
State-Level Trends in Real Income Per Capita and Income Inequality, 1945–2004

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where \( \lambda_{i,j} = \alpha_{i,j} \forall j \neq 1 \) and \( \lambda_{i,1} = \alpha_{i,1} + 1 \).

Real state income per capita \( (y_{i,t}) \) is taken from the Regional Accounts Data available at the Web site of the Bureau of Economic Analysis (BEA) and deflated using the consumer price index (2004 = 100).\(^5\) We also include two measures of human capital attainment in vector \( X_{i,t} \): the proportion of the population with at least a high school degree and the proportion with at least a college degree. The inclusion of these measures is consistent with much of the relevant theoretical literature (Aghion and Bolton 1997; Galor and Moav 2004; Galor and Zeira 1993; Perotti 1993). Human capital attainment information is unavailable on an annual state-level basis for much of our early sample period, however. We therefore constructed measures of human capital attainment using the perpetual inventory method proposed by Barro and Lee (1993, 1996, 2000). Appendix B describes this construction and provides tests of its accuracy.

Estimation of the model is problematic, however, if the log of real income per capita and income inequality are nonstationary. For \( \varepsilon_{i,t} \) to be stationary, it must be the case that any \( I(1) \) variables are cointegrated. Nonstationarity appears likely as given in Figures I and 2, where each series appears to meander, and shows no tendency to return to a constant mean over the 60-yr period. We formally test for nonstationarity using several Hadri (2000) panel stationarity tests. In each test, the null hypothesis of stationarity is rejected at the 1% significance level.\(^6\) This finding is consistent with nonstationary results we found using the U.S. time-series inequality data of Piketty and Saez (2003) for the period 1913–1998.\(^7\)

To evaluate if the variables are cointegrated, we employ the Kao (1999) test, an augmented Dickey-Fuller-type test applicable to panel data, as well as the Pedroni (1995, 2004) test and a pooled Phillips and Perron-type test for panel data. Note that cointegration is implied if a long-run relationship between real income per capita and income inequality exists. With both these cointegration tests, we reject the null hypothesis of no cointegration at the 1% significance level.\(^8\)

Equation (2) can be reparameterized into the error-correction equation:

\[
\Delta y_{i,t} = \phi_{i} (y_{i,t-1} - \theta_{i} X_{i,t}) + \sum_{j=1}^{p-1} \lambda_{ij} \Delta y_{i,t-j} + \sum_{j=0}^{q-1} \beta_{ij} \Delta X_{i,t-j} + \mu_{t} + \tau_{t} + \varepsilon_{i,t},
\]

where

\[
\phi_{i} = -\left(1 - \sum_{j=1}^{p} \delta_{j}\right),
\]

\[
\theta_{i} = \sum_{j=0}^{q} \beta_{ij} - \sum_{k} \lambda_{ik},
\]

\[
\lambda_{ij} = -\sum_{m=j+1}^{p} \lambda_{im},
\]

\[
\beta_{ij} = -\sum_{m=j+1}^{q} \beta_{im}.
\]

7. We evaluated each of the data series presented in Figures I and II of Piketty and Saez (2003): income shares for the top 90%-100% (P90-100), the top 90%-95% (P90-95), the top 95%-99% (P95-99), and the top 99%-100% (P99-100). Under the null hypothesis of a unit root, the augmented Dickey-Fuller test statistic for P90-100 is \(-1.096\), for P90-95 the test statistic is \(-2.814\), for P95-99 the test statistic is \(-1.765\), and for P99-00 the test statistic is \(-1.810\). Each of these test statistics is insignificant at the 5% level (5% critical value = \(-2.908\)), indicating the presence of a unit root in each series. Phillips-Perron unit root tests also indicate nonstationarity in each of the four series.

8. The Kao (1999) test statistic for the null hypothesis of no cointegration between log real income per capita and the top decile share of income is \(-6.44\), while the Pedroni (1995, 2004) test statistic is \(-16.97\). The Kao test statistic for no cointegration between log real income per capita, top decile share of income, high school attainment, and college attainment is \(-3.36\), while the Pedroni test statistic is \(-15.38\). Each of the above tests is statistically significant at the 1% level.
The parameter $\phi_i$ is the error-correcting speed of adjustment term; the vector $\theta'$ captures the long-run relationships between the variables, while $\beta'_{ij}$ captures the short-run relationships. One would expect the parameter $\phi_i$ to be significantly negative if the variables show a return to long-run equilibrium. If $\phi_i = 0$, however, there would be no evidence for a long-run relationship. Since we are primarily interested in the nature of the long-run relationship between growth and income inequality, the long-run vector of coefficients $\theta'$ will be of particular importance.

From Equation (3), the fixed time effects ($\tau_i$) can be eliminated by mean-differencing the variables from their cross-section means. Eliminating the time effects is important given the long span of the sample and the year-to-year incremental changes in tax laws associated with IRS income data. Additionally, the fixed state effects ($\mu_j$) can be eliminated by estimating Equation (3) with the FE estimator. With the FE estimator, the time-series data for each state are pooled and only the intercepts are allowed to differ across states. If the slope coefficients are not identical, however, the FE estimator could produce inconsistent and potentially misleading results. Moreover, Li, Squire, and Zou (1998), Barro (2000), and Quah (2001) have argued against the use of FE, at least in the international context, since much of the variation in international inequality is cross-sectional. Their contention is that the use of the FE estimator would incorrectly lead to the conclusion of an insignificant relationship since much of the variation in international income inequality occurs over the cross-sectional dimension. Partridge (2005) implies that a similar variation may exist in state-level inequality panels, though we do not find evidence of a cross-sectional weight in our inequality panel.9

Alternatively, Equation (3) could be estimated for each state separately, and an average of the coefficients could then be calculated. This is the MG estimator proposed by Pesaran and Smith (1995). The MG estimator exploits the unusually large number of time-series observations available for each state and provides an important alternative to the FE estimator. With the MG estimator, for example, the error-correction speed of adjustment term is

$$\hat{\phi}_{MG} = N^{-1} \sum_{i=1}^{N} \hat{\phi}_i$$

with the variance

$$\hat{\delta}_{MG} = \frac{1}{N(N-1)} \sum_{i=1}^{N} (\hat{\phi}_i - \bar{\phi})^2.$$ 

Since the intercepts, slope coefficients, and error variances are all allowed to differ across states, the cross-sectional information of the data will be retained. This is a useful feature given the aforementioned concerns of Li, Squire, and Zou (1998), Barro (2000), and Quah (2001).

More recently, Pesaran, Shin, and Smith (1999) have proposed a third alternative, the pooled MG estimator, which combines both pooling and averaging. This intermediate estimator allows the intercepts, short-run coefficients, and error variances to differ across states (as would the MG estimator) but pools the data and constrains the long-run coefficients to be the same across states (as would an FE estimator). Since Equation (3) is nonlinear in the parameters, Pesaran, Shin, and Smith (1999) develop a maximum likelihood method to estimate the parameters. Expressing the likelihood as the product of each cross-section’s likelihood and taking the log yields:

$$I_T(\theta', \varphi', \sigma') = -\frac{T}{2} \sum_{i=1}^{N} \ln 2\pi \sigma_i^2$$

$$- \frac{1}{2} \sum_{i=1}^{N} \frac{1}{\sigma_i^2} (\Delta y_i - \bar{\phi}_i \bar{\xi}_i(0))$$

for $i = 1, 2, \ldots, N$, where $\bar{\xi}_i(0) = y_{i, t-1} - X_i \theta_0$, $H_i = I_T - W_i(W_i'W_i)^{-1}W_i$, $I_T$ is the identity
matrix of order $T$, and $W_t = (\Delta y_{it-1}, \ldots, \Delta y_{it-p+1}, \Delta y_{it}, \Delta x_{it}, \ldots, \Delta x_{it-q+1})$. The likelihood is maximized iteratively via back-substitution until convergence is achieved.¹⁰

Table 2 presents our primary estimates of the relationship between income inequality and human capital attainment on economic growth. Ten additional industry wage and salary variables are also included in each estimation as short-run control variables.¹¹ In the first three models, the ARDL (1,1) form of Equation (3) is estimated via the dynamic FE, pooled MG, and MG estimators. In the final two models, the Schwarz Bayesian Criterion (SBC) is used to select the lag lengths for the pooled MG and MG estimators. Across all the models, the long-run relationship between the top decile share of income and economic growth is positive and statistically significant. Notice that the magnitude of the relationship is similar across the estimators (dynamic FE, pooled MG, and MG), suggesting that U.S. inequality panels are not as sensitive to the use of an FE estimator as international panels (Barro 2000; Li, Squire, and Zou 1998; Quah 2001). The magnitude is impacted by the selection of lags, however, with the more parsimonious ARDL (1,1) specification (Columns 1–3) indicating a relationship of larger magnitude than the SBC models (Columns 4 and 5).

In the estimations in Table 2, the speed of adjustment parameter, $\phi_i$, is consistently negative and significant but does vary in magnitude. While the MG and pooled MG $\phi_i$ indicate similar returns to long-run equilibrium, the dynamic FE $\phi_i$ implies a much slower return. The two long-run human capital variables are always positive in sign, as expected, though not always statistically significant.¹² This lack of significance is well

¹⁰. To estimate the FE, MG, and pooled MG estimators using Stata, see Blackburne and Frank (2007).
¹¹. These data are taken from the Regional Economic Accounts data available at the Web site of the BEA.
¹². Notice also that the two short-run human capital coefficients are always negatively signed, as one would expect given the temporal trade-off inherent in educational investment.
known in the human capital literature (Krueger and Lindahl 2001) and the continuing subject of recent research (see, e.g., Vandenbussche, Aghion, and Meghir 2006).

To evaluate the differences between the MG and the pooled MG estimations, note that the long-run coefficients from the pooled MG estimator are restricted to be the same for all states, while the MG long-run coefficients are unrestricted. To compare these two estimators, a Hausman test can be performed to test the additional restrictions of the pooled MG estimator (Pesaran, Shin, and Smith 1999). Under the null hypothesis of the Hausman test, there are no differences in the estimators; thus, the pooled estimator is consistent and efficient. In the ARDL estimations of Table 2 (Columns 2 and 3), the Hausman test statistic is a marginally insignificant 6.76 (p value = .08). Similarly, in the SBC estimations (Columns 4 and 5), the Hausman test statistic is 6.87 (p value = .08). Hence, the pooled MG estimates appear consistent and efficient in comparison to the unrestricted MG estimation.

To further interpret this relationship between inequality and economic growth, notice from the pooled MG ARDL parameter estimates (Column 2) that a two–standard deviation increase in the top decile share of income (about 0.09, Table 1) would be related to an increase in the long-run growth rate of real income per capita of 0.072% ceteris paribus.

Table 3 continues this evaluation by replicating the pooled MG estimation from Column 2 of Table 2 with six alternative measures of inequality. The first two columns divide the top decile into two groups: the income share of the top 1% (Column 1) and the income share of the top 90%–99% (Column 2). An interesting relationship emerges; the positive long-run association between inequality and growth is found to reside only within the income share of the top 1%, while the income share of the top 90%–99% appears to have no significant relation to economic growth. The parameter estimates from Column 1 of Table 3 imply that a two–standard deviation increase in the share of income of the top 1% would increase the long-run growth rate of real income per capita by 0.066%.

Column 3 of Table 3 replaces the percentile share of income measures with the gini coeffic-

| TABLE 3 |
|-----------------|-----------------|-----------------|-----------------|-----------------|
| Alternative Inequality Measures of Economic Growth and Income Inequality | Top 1% | Top 90%–99% | Gini Coefficient |
|-----------------|-----------------|-----------------|-----------------|-----------------|
| Atkinson Index, ϵ = 0 | -0.588* (0.038) | -0.582* (0.036) | -0.582* (0.036) |
| Atkinson Index, ϵ = 1 | 0.703* (0.044) | 0.689 (0.091) | 0.689 (0.091) |
| Theil Entropy Index | 0.036 (0.078) | 0.036 (0.078) | 0.036 (0.078) |
| Adjusting coefficient (θ) | 0.724 (0.126) | 0.724 (0.126) | 0.724 (0.126) |

Notes: Standard errors are in parentheses. All variables are mean-differenced. Short-run coefficients are included in each estimation but not reported in the table. Each model is estimated using the dynamic panel data correction pooling MG estimator and includes ten short-run industry wage and salary variables.

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cient, a measure of inequality which encompasses the entire income distribution. Again the long-run relationship between inequality and economic growth is positive and statistically significant, though the magnitude of the relationship appears considerably smaller than the relationship found using the top 10% and top 1% measures of inequality. The estimates from Column 3 imply that a two-standard deviation increase in the gini coefficient would be related to a 0.008% increase in the long-run growth rate of real income per capita. One possible explanation for this difference in magnitude is that the true relationship between inequality and growth is narrowly related to only upper end income inequality. Hence, the smaller magnitude from the gini coefficient would be a meaningful difference driven by the broad nature of inequality captured by the gini coefficient. Alternatively, it is plausible that the gini coefficient is an inefficient measure of inequality in the context of IRS income data, since IRS data are truncated below a threshold level of income, as discussed in the previous section.

The next two columns use the Atkinson index of inequality, a measure of inequality bound between 0 and 1, with higher values indicating greater inequality. Column 4 employs an inequality aversion parameter (e) of 0.5, meaning the index is sensitive to transfers to those in the high end of the income distribution. Column 5, by contrast, uses an inequality aversion parameter of 1.5, meaning the index is sensitive to transfers at the low end of the distribution. Both measures indicate that income inequality is positively related to economic growth. Moreover, the parameter estimates in Column 4 imply that a two-standard deviation increase in inequality from the high-aversion Atkinson index will be related to an increase in the long-run growth rate of real income per capita of 0.063%, a magnitude very similar to the top decile and top 1% income share measures discussed above. By contrast, the low-aversion Atkinson index in Column 5 indicates that a two-standard deviation increase in inequality will be related to only a 0.023% increase in the long-run growth.

Combined with the top 1% and top 90%-99% income share findings (Columns 1 and 2), these Atkinson index results provide further evidence that the positive relationship between inequality and growth is driven principally by the concentration of income in the upper end of the income distribution. The relationship between bottom-end inequality and economic growth remains an open question, however. It is noteworthy that Voitchovsky (2005) has found evidence that while top-end inequality is positively associated with growth, bottom-end inequality may be negatively related to growth. IRS income data, however, are not well suited for the construction of bottom-end inequality measures given the truncation of low-income individuals.

IV. CONCLUSIONS

This paper is motivated by the desire to provide a comprehensive state-level panel of income inequality measures covering the entirety of the postwar period. Existing state-level and cross-national inequality panels are often restricted to only recent years or contain only a very limited number of time-series observations for each cross-section. Panels that cover the entirety of the postwar period are typically spaced at 10-yr intervals, meaning that only five or six time-series observations are available for each cross section. This paper, by contrast, offers a new comprehensive panel of annual income inequality measures for the 48 states over the 60-yr period 1945–2004. These measures of inequality are constructed from individual tax filing data available from the IRS. Although IRS income data have several important limitations, including the censoring of individuals...
below a threshold level of income, they have the unique feature of being available annually for each state throughout the postwar period.

Individual state-level trends in income inequality from this panel appear to closely replicate the overall trends in aggregate U.S. inequality found by Piketty and Saez (2003). For the vast majority of states, the share of income held by the top decile experienced a prolonged period of stability after World War II, followed by a substantial increase in inequality during the 1980s and 1990s.

This paper also offers an exploration of the long-run relationship between income inequality and economic growth. Given the unusually large and balanced size of our panel, we have employed three alternative dynamic panel error-correction estimators: the FE estimator, the MG estimator of Pesaran and Smith (1995), and the pooled MG estimator of Pesaran, Shin, and Smith (1999). From this analysis, we find the long-run relationship between income inequality and economic growth to be positive in nature. The results imply that a two-standard deviation increase in the top 10% share of income is related to an increase in the long-run growth rate of real income per capita of 0.072%.

the current inequality-growth literature, for example, uses a 10- or 20-yr lag between inequality and subsequent economic growth rates (Barro 2000; Forbes 2000; Panizza 2002; Partridge 1997, 2003). This practice reflects the desire to isolate the long-run relationship between inequality and growth but is also an imposed artifact of prior data limitations. The new inequality panel this paper introduces, unlike the low-frequency panels of prior research, has both the comprehensiveness and the flexibility to further the empirical evaluation of each of these concerns.

APPENDIX A: CONSTRUCTION OF THE INEQUALITY MEASURES

The income inequality measures are constructed using data published by the IRS on the number of returns and adjusted gross income (before taxes) by state and size of the adjusted gross income. Percentile rankings are used to construct the top decile share of income. This construction is based on the split-histogram interpolation method suggested by Cowell (1995), whereby the proportion of the population with income less than or equal to income $y$ is defined as:

$$F(y) = F_i + \int_y^\infty \Phi_i(x) dx,$$

where $a_i$ is the lower bound of group $i$ and $F_i$ is the cumulative frequency of the number of individuals before group $i$. The proportion of the total income received by those with income less than or equal to $y$ is given by

$$\Phi(y) = \Phi_i + \frac{1}{\mu} \int_{a_i}^y x \Phi_i(x) dx,$$

where $\mu$ is mean income. The density within each interval $i$ is defined by the split-histogram density:

$$\phi_i = \begin{cases} 
\frac{f_i(a_{i+1} - a_i)}{(a_{i+1} - a_i)({\mu_i} - a_i)}, & \text{for } a_i \leq x \leq \mu_i \\
\frac{f_i(a_{i+1} - a_i)}{(a_{i+1} - a_i)(a_{i+1} - {\mu_i})}, & \text{for } \mu_i \leq x \leq a_{i+1}
\end{cases}$$

14. Banerjee and Duflo (2003), for example, argue the political-economy mechanism (whereby voters respond to increased inequality with harmful redistribution) is limited by important time lags, leading to substantial differences between the short-run and long-run inequality-growth relationship.
where \( f_i \) is the relative frequency of \( n_i \) within group \( i \), and \( a_{i+1} \) is the upper bound of group \( i \). Since the IRS income data are in group form, the gini coefficient we construct is the compromise gini coefficient proposed by Cowell and Mehta (1982) and Cowell (1995). Accordingly, the lower limit of the gini can be derived based on the assumption that all individuals in a group receive exactly the mean income of the group:

\[
G_L = \frac{1}{2} \sum_{i=1}^{k} \sum_{j=1}^{k} n_i n_j (\mu_i - \mu_j),
\]

where \( n \) is the number of individuals and subscripts \( i \) and \( j \) denote within-group values. The upper limit gini can be constructed based on the assumption that individuals within the group receive income equal to either the lower or the upper bound of the group interval:

\[
G_U = G_L + \sum_{i=1}^{k} \frac{n_i^2(a_{i+1} - \mu_i)(\mu_i - a_i)}{n_i^2\mu_i(a_{i+1} - a_i)}.
\]

The compromise gini coefficient proposed by Cowell and Mehta (1982) is simply \( G_U = G_L + G_L / 3.\)

The Atkinson index and Theil entropy index can be derived using the basic form:

\[
J = \sum_{i=1}^{k} a_{i+1} h(y) \phi_i(y) dy,
\]

where \( \phi_i \) is the split-histogram density and \( h(y) \) is an evaluation function. To construct the Atkinson index, the evaluation function is defined as:

\[
h(y) = \left( \frac{y}{\mu} \right)^{1-\varepsilon},
\]

where \( 1 - J^{1/1-\varepsilon} \). Note that \( \varepsilon \) is the Atkinson inequality aversion parameter. To construct the Theil entropy index, the evaluation function is given by:

\[
h(y) = \frac{y}{\mu} \ln \left( \frac{y}{\mu} \right).
\]

Unlike the percentile rankings or gini index, the Atkinson index and Theil index are undefined for negative incomes (Cowell 1995). Hence, to construct the Atkinson and Theil inequality measures, negative IRS income data must be truncated, meaning the lowest possible income, \( a_1 \), is $0.

**B. CONSTRUCTION OF THE HUMAN CAPITAL MEASURES**


To build an annual state-level measure of human capital attainment, we follow the spirit of the perpetual inventory method proposed by Barro and Lee (1993, 1996, 2000). Attainment information from the Census and March CPS is used as benchmark human capital stocks, while the number of new graduates each year is used as flows added to the current stock of human capital. Additionally, each year’s stock is adjusted for mortality and net migration. Accordingly, we construct two human capital attainment-to-population ratios for each state:

\[
(\text{B.1}) \quad \text{high school}_t = \frac{h_{i,t}}{n_{i,t}} = \frac{(n_{i,t-1} - d_{i,t} + m_{i,t}) \text{high school}_{t-1} + h_{i,t}}{n_{i,t}}
\]

and

\[
(\text{B.2}) \quad \text{college}_t = \frac{c_{i,t}}{n_{i,t}} = \frac{(n_{i,t-1} - d_{i,t} + m_{i,t}) \text{college}_{t-1} + h_{i,t}}{n_{i,t}}
\]

where \( h_{i,t} \) is the total number of individuals with at least a high school diploma in state \( i \) for year \( t \), \( c_{i,t} \) is the total number of individuals with at least a baccalaureate or first professional degree, \( h_{i,t} \) is the number of new high school graduates, \( c_{i,t} \) is the number of new bachelor or first professional degrees conferred, \( d_{i,t} \) is the number of deaths, and \( m_{i,t} \) is net migration (the number of new arrivals into a state minus the number that have left the state).

The assumption from Equations (B.1) and (B.2) is that the number of deaths and net migration are independent from the level of schooling attained. Though not entirely accurate, this assumption is necessary given data limitations and similar to the assumption made by Barro and Lee (1993, 1996, 2000).

Net migration \( (m_{i,t}) \) is not known on an annual basis for each state but may be inferred, since the change in population from period \( t - 1 \) to period \( t \) must equal the number of new births minus the number of deaths plus net migration:

\[
(\text{B.3}) \quad n_{i,t} - n_{i,t-1} = b_{i,t} - d_{i,t} + m_{i,t}.
\]

Rearranging Equation (B.3) and substituting into Equations (B.1) and (B.2),

\[
(\text{B.4}) \quad \text{high school}_t = \frac{(n_{i,t} - b_{i,t}) \text{high school}_{t-1} + h_{i,t}}{n_{i,t}}
\]

and

\[
(\text{B.5}) \quad \text{college}_t = \frac{(n_{i,t} - b_{i,t}) \text{college}_{t-1} + h_{i,t}}{n_{i,t}}.
\]

16. The population 25 and older, a more intuitive denominator, is not available annually at the state level for the entirety of the sample period.
Equations (B.4) and (B.5) may then be used to construct forward-flow and backward-flow estimates of human capital attainment for the missing cells (65.2% of the sample). As a rule, we choose the flow estimate that minimizes the distance from a Census or March CPS benchmark. For the year 1967, for example, the backward-flow estimate is used since the 1970 Census benchmark is closer than the 1960 benchmark. In years where the backward-flow and forward-flow estimates are equal distances apart (e.g., 1965), an average of the two is used.

To evaluate the accuracy of our perpetual inventory method, we estimate attainment over the period 1979–2004 using only the Census benchmark information (1980, 1990, and 2000) and compare these values to the actual attainment information provided in the March CPS. The root mean square error of the actual and estimated is 0.022 for high school attainment and 0.013 for college attainment. Following Barro and Lee (1993), we can further assess this accuracy using the Theil statistic, a measure bound between 0 and 1, with larger values indicating poor forecasting performance. Over this period, the Theil statistic for high school attainment is 0.043, a magnitude substantially less than the secondary attainment measures of Barro and Lee (0.14–0.36). Similarly, the Theil statistic for college attainment is 0.087, a magnitude less than the higher attainment measures of Barro and Lee (0.10–0.25). Both values indicate that the two attainment measures provide a good fit for the period sampled, though the high school attainment measure performs better than the college attainment measure. It is plausible that this difference in relative performance reflects the greater mobility of college graduates vis-à-vis high school graduates, a tendency we are unable to account for.

REFERENCES

17. For the years 1963–2004, the annual number of college graduates (bachelor’s and first professional degrees) and public high school graduates are available from annual issues of the Digest of Educational Statistics and the Statistical Abstract of the United States. For the years 1945–1962, the Biennial Survey of Education and the Statistical Abstract of the United States are used. The years 1953, 1955, and 1961 were undocumented and thus had to be linearly interpolated. The number of live births and total population are available from annual issues of the Statistical Abstract of the United States.


