

## ERRATA

### Abstract Algebra, Third Edition

by D. Dummit and R. Foote

(most recently revised on March 4, 2009)

These are errata for the Third Edition of the book. Errata from previous editions have been fixed in this edition so users of this edition do not need to refer to errata files for the Second Edition (on this web site). Individuals using the Second Edition, however, must make corrections from this list as well as those in the Second Edition errata files (except for corrections to text only needed in the Third Edition; for such text no reference to Second Edition page numbers is given below). Some of these corrections have already been incorporated into recent printings of the Third Edition.

**page vi (2<sup>nd</sup> Edition p. vi)**

*from:* 7.3 Ring Homomorphisms and Quotient Rings

*to:* 7.3 Ring Homomorphisms and Quotient Rings

**page 2, Proposition 1(1) (2<sup>nd</sup> Edition p. 2, Proposition 1(1))**

*from:* The map  $f$  is injective

*to:* If  $A$  is not empty, the map  $f$  is injective

**page 4, line -3 (2<sup>nd</sup> Edition p. 5, line 3)**

*from:*  $a, b \in \mathbb{Z} - \{0\}$

*to:*  $a, b \in \mathbb{Z}$  and  $b \neq 0$

**page 31, The group  $S_3$  table**

*last line missing*

*add:*  $\sigma_6(1) = 3, \sigma_6(2) = 1, \sigma_6(3) = 2$      |      $(1\ 3\ 2)$

**page 33, Exercise 10, line 2 (2<sup>nd</sup> Edition p. 33, Exercise 10)**

*from:* its least residue mod  $m$  when  $k + i > m$

*to:* its least positive residue mod  $m$

**page 34, line 1 of Definition (2<sup>nd</sup> Edition p. 34, line 1 of Definition)**

*from:* two binary operations

*to:* two commutative binary operations

**page 39, Example 2, line -4**

*from:*  $ba = ab^{-1}$

*to:*  $ba = a^{-1}b$

**page 45, Exercise 22 (2<sup>nd</sup> Edition p. 46, Exercise 22)**

*from:* is isomorphic to a subgroup (cf. Exercise 26 of Section 1) of  $S_4$

*to:* is isomorphic to  $S_4$

**page 51, line -1 (2<sup>nd</sup> Edition p. 52, line -1)**

*from:* see Exercise 1 in Section 1.7

*to:* see Exercise 4(b) in Section 1.7

**page 65, line 2 of Exercise 16(c) (2<sup>nd</sup> Edition p. 66, Exercise 16(c))**

*from:* if and only  $H$

*to:* if and only if  $H$

**page 71, Exercise 5 (2<sup>nd</sup> Edition p. 72, Exercise 5)**

*from:* there are 16 such elements  $x$

*to:* there are 8 such elements  $x$

**page 84, line 11 of Example 2 (2<sup>nd</sup> Edition p. 85, line 11 of Example 2)**

*from:* By Proposition 2.6

*to:* By Theorem 2.7(1)

**page 84, line -6 of Example 2 (2<sup>nd</sup> Edition p. 85, line -6 of Example 2)**

*from:* By Proposition 2.5

*to:* By Theorem 2.7(3)

**page 98, Figure 6**

*add:* hatch marks to upper right and lower left lines of the central diamond (to indicate  $AB/B \cong A/A \cap B$ ).

**page 103, line 3 of Definition (2<sup>nd</sup> Edition p. 104, line 3 of Definition)**

*from:*  $N_{i+1}/N_i$  a simple group

*to:*  $N_{i+1}/N_i$  is a simple group

**page 114, line 3 in proof of Proposition 2 (2<sup>nd</sup> Edition p. 116, line 3 of proof)**

*from:*  $b \in G$

*to:*  $g \in G$

**page 132, Exercise 33, line -1 (2<sup>nd</sup> Edition p. 134, line -1 of Exercise 33)**

*from:* See Exercises 6 and 7 in Section 1.3

*to:* See Exercises 16 and 17 in Section 1.3

**page 132, Exercise 36(c) (2<sup>nd</sup> Edition p. 135, Exercise 36(c))**

*from:*  $g$  and  $h$  lie in the center of  $G$

*to:*  $g$  and  $h$  lie in the center of  $G$  and  $g = h^{-1}$

**page 139, Definition (1) (2<sup>nd</sup> Edition p. 141, Definition (1))**

*from:* A group of order  $p^\alpha$  for some  $\alpha \geq 1$

*to:* A group of order  $p^\alpha$  for some  $\alpha \geq 0$

**page 143, last line of first Example (2<sup>nd</sup> Edition p. 145, line -2)**

*from:* Theorem 17

*to:* Proposition 17

**page 148, Exercise 47(i) (2<sup>nd</sup> Edition p. 151, Exercise 47(i))**

*from:* that has some prime divisor  $p$  such that  $n_p$  is not forced to be 1

*to:* for each prime divisor  $p$  of  $n$  the corresponding  $n_p$  is not forced to be 1

**page 149, Exercise 54, line 4 (2<sup>nd</sup> Edition p. 151, line 4 of Exercise 54)**

*from:*  $G/N$  acts as automorphisms of  $N$

*to:*  $G/C_G(N)$  acts as automorphisms of  $N$

**page 151, Exercise 6, line –2 (2<sup>nd</sup> Edition p. 153, line –2 of Exercise 6)**

*from:* every pair of elements of  $D$  lie in a finite simple subgroup of  $D$

*to:* every pair of elements of  $A$  lie in a finite simple subgroup of  $A$

**page 158, line 3 after the Definition (2<sup>nd</sup> Edition p. 160)**

*from:*  $n$ -tuple

*to:*  $r$ -tuple

**page 187, Exercise 23, line 4 (2<sup>nd</sup> Edition p. 189, line 4 of Exercise 23)**

*from:* from  $G$  into

*to:* from  $K$  into

**page 191, Proposition 2 (2<sup>nd</sup> Edition p. 193, Proposition 2)**

*from:* nilpotence class at most  $a - 1$ .

*to:* nilpotence class at most  $a - 1$  for  $a \geq 2$  (and class equal to  $a$  when  $a = 0$  or  $1$ ).

**page 191, line 3 of the proof of Proposition 2 (2<sup>nd</sup> Edition p. 193)**

*from:* Thus if  $Z_i(P) \neq G$

*to:* Thus if  $Z_i(P) \neq P$

**page 194, Theorem 8, line 4 (2<sup>nd</sup> Edition p. 196, Theorem 8, line 4)**

*from:*  $Z_i(G) \leq G^{c-i-1} \leq Z_{i+1}(G)$  for all  $i \in \{0, 1, \dots, c-1\}$ .

*to:*  $G^{c-i} \leq Z_i(G)$  for all  $i \in \{0, 1, \dots, c\}$ .

**page 198, Exercise 18 (2<sup>nd</sup> Edition p. 200, Exercise 18)**

*from:* then  $G'' = 1$

*to:* then  $G'' = G'''$

**page 199, Exercise 22 (2<sup>nd</sup> Edition p. 201, Exercise 22)**

*from:* Prove that

*to:* When  $G$  is a finite group prove that

**page 201, line 2 of Exercise 38 (2<sup>nd</sup> Edition p. 203, Exercise 38)**

*from:* The group  $G/M$

*to:* The group  $P/M$

**page 209, Proposition 14(1)**

*from:*  $n_3 = 7$

*to:*  $n_3 = 28$

**page 216, line 4 after displayed steps (1) and (2) (2<sup>nd</sup> Edition p. 217, line –3)**

*from:* are equal if and only if  $n = m$  and  $\delta_i = \epsilon_i$ ,  $1 \leq i \leq n$

*to:* are equal if and only if  $n = m$ ,  $r_i = s_i$  and  $\delta_i = \epsilon_i$ ,  $1 \leq i \leq n$

**page 260, Exercise 40(iii) (2<sup>nd</sup> Edition p. 261, Exercise 40(iii))**

*from:*  $R/\eta(R)$

*to:*  $R/\mathfrak{N}(R)$

**page 263, line 2 of the Definition (2<sup>nd</sup> Edition p. 264)**

*from:* ring of fractions of  $D$  with respect to  $R$   
*to:* ring of fractions of  $R$  with respect to  $D$

**page 269, line 2 of Exercise 10(c) (2<sup>nd</sup> Edition p. 270, Exercise 10(c))**

*from:* then  $A$  may likewise  
*to:* then  $P$  may likewise

**page 269, line 2 of Exercise 11(d) (2<sup>nd</sup> Edition p. 270, Exercise 11(d))**

*from:* Prove that every ideal of  
*to:* Prove that every nonzero ideal of

**page 269, lines 1 and 2 of Exercise 11(e) (2<sup>nd</sup> Edition p. 270, Exercise 11(e))**

*from:* in the direct limit  $\mathbb{Z}_p$  satisfying  $a_j^p$   
*to:* in the inverse limit  $\mathbb{Z}_p$  satisfying  $a_j^{p-1}$

**page 282, second display (2<sup>nd</sup> Edition p. 283, second display)**

$$\text{from: } 0 < N\left(\frac{\alpha}{\beta}s - t\right) = \frac{(ay - 19bx - cq)^2 + 19(ax + by + cz)^2}{c^2} \leq \frac{1}{4} + \frac{19}{c^2}$$

and so (\*) is satisfied with this  $s$  and  $t$  provided  $c \geq 5$ .

$$\text{to: } 0 < N\left(\frac{\alpha}{\beta}s - t\right) = \frac{(ay - 19bx - cq)^2 + 19(ax + by + cz)^2}{c^2} = \frac{r^2 + 19}{c^2} \leq \frac{1}{4} + \frac{19}{c^2}$$

and so (\*) is satisfied with this  $s$  and  $t$  provided  $c \geq 5$  (note  $r^2 + 19 \leq 23$  when  $c = 5$ ).

**page 283, Exercise 8 (2<sup>nd</sup> Edition p. 284, Exercise 8)**

*from:*  $D$  is a multiplicatively closed subset of  $R$   
*to:*  $D$  is a multiplicatively closed subset of  $R$  with  $0 \notin D$

**page 290, line 5 (2<sup>nd</sup> Edition p. 291, line 5)**

*from:* is irreducible in  $\mathbb{Z}[i]$   
*to:* is irreducible in  $\mathcal{O}$

**page 304, line 13 (2<sup>nd</sup> Edition p. 305, line 3)**

*from:* one fewer irreducible factors  
*to:* one fewer irreducible factor

**page 306, line 3 (2<sup>nd</sup> Edition p. 307, line 3)**

*from:* where  $p'(x)$  is irreducible in both  $R[x]$  and  $F[x]$ .  
*to:* where  $p'(x)$  is irreducible in  $R[x]$  if and only if it is irreducible in  $F[x]$ .

**page 312, Exercise 16(b) (2<sup>nd</sup> Edition p. 313, Exercise 16(b))**

*from:* Prove that  $f$   
*to:* If  $f(0) \neq 0$ , prove that  $f$

**page 318, line 7 after the Definition**

*from:*  $L(fg) = L(f) + L(g)$   
*to:*  $L(fg) = L(f)L(g)$

**page 323, line –6***from:* among the differences  $S(g_i, g_j)$ *to:* among the remainders of the differences  $S(g_i, g_j)$ **page 331, Exercise 3(i)***from:* minimum element*to:* minimal element**page 332, Exercise 9(b)***from:* grlex order*to:* grevlex order**page 332, Exercise 15(a)***from:* Prove that  $\{g_1, \dots, g_m\}$  is a minimal Gröbner basis for the ideal  $I$  in  $R$  if*to:* Prove that the subset  $\{g_1, \dots, g_m\}$  of the ideal  $I$  in  $R$  is a minimal Gröbner basis of  $I$  if**page 332, Exercise 16, line 3***from:*  $(LT(g_1), \dots, LT(g_m), LT(S(g_i, g_j)))$  is strictly larger than the ideal  $(LT(g_1), \dots, LT(g_m))$ .  
Conclude that the algorithm ...*to:*  $(LT(g_1), \dots, LT(g_m), LT(r))$  is strictly larger than the ideal  $(LT(g_1), \dots, LT(g_m))$ , where  $S(g_i, g_j) \equiv r \pmod{G}$ . Deduce that the algorithm ...**page 333, display in Definition following Exercise 33***from:*  $rJ \in I$ *to:*  $rJ \subseteq I$ **page 334, Exercise 43(a)***from:* Use Exercise 30*to:* Use Exercise 39**page 334, Exercise 43(b)***from:* Use Exercise 33(a)*to:* Use Exercise 42(a)**page 334, line 3 of Exercise 43(c)***from:* ideal defined in Exercise 32,*to:* ideal quotient (cf. Exercise 41),**page 348, line 6 (2<sup>nd</sup> Edition p. 329, line 6)***from:* When  $R$  is a field, however*to:* When  $R$  is a field and  $M \neq 0$ , however**page 350, line 2 of Exercise 4 (2<sup>nd</sup> Edition p. 331, Exercise 4)***from:*  $\varphi(\bar{k}) = ka$ *to:*  $\varphi_a(\bar{k}) = ka$ **page 357, Exercise 21(i) (2<sup>nd</sup> Edition p. 338, Exercise 21(i))***replace (i) with:* the map from the (external) direct sum  $\bigoplus_{i \in I} N_i$  to the submodule of  $M$  generated by all the  $N_i$ 's by sending a tuple to the sum of its components is an isomorphism (cf. Exercise 20)

**page 372, Corollary 16(2), top line of commutative diagram**

$$\begin{array}{l} \text{from: } M \times \cdots \times M_n \xrightarrow{\iota} M \otimes \cdots \otimes M_n \\ \text{to: } M_1 \times \cdots \times M_n \xrightarrow{\iota} M_1 \otimes \cdots \otimes M_n \end{array}$$

**page 374, line 2 of second Remark (2<sup>nd</sup> Edition p. 355 line 2)**

*from:* Section 11.6  
*to:* Section 11.5

**page 375, line 4 of Exercise 8 (2<sup>nd</sup> Edition p. 356, Exercise 8)**

*from:* relation  $(u, n) \sim (u', n)$  if and only if  $u'n = un'$  in  $N$ .  
*to:* relation  $(u, n) \sim (u', n')$  if and only if  $xu'n = xun'$  in  $N$  for some  $x \in U$ .

**page 377, Exercise 23 (2<sup>nd</sup> Edition p. 357, Exercise 23)**

*from:* Proposition 19  
*to:* Proposition 21

**page 385, title of subsection following Proposition 26**

*from:* Modules and  $\text{Hom}_R(D, -)$   
*to:* Projective Modules and  $\text{Hom}_R(D, -)$

**page 396, line -2 above Proposition 36 (2<sup>nd</sup> Edition p. 376)**

*from:* Exercises 18 and 19  
*to:* Exercises 19 and 20

**page 398, proof of Theorem 38 (2<sup>nd</sup> Edition p. 378)**

*from:* Exercises 15 to 17  
*to:* Exercises 15 and 16

**page 399, line 8 (2<sup>nd</sup> Edition p. 379, line 22)**

*from:* The map  $1 \otimes \varphi$  is not in general injective  
*to:* The map  $1 \otimes \psi$  is not in general injective

**page 401, line 2 of Example 1 (2<sup>nd</sup> Edition p. 381, line 2 of Example 1 )**

*from:*  $\mathbb{Z}/2\mathbb{Z}$  not a flat module  
*to:*  $\mathbb{Z}/2\mathbb{Z}$  is not a flat module

**page 403, Exercise 1(d) (2<sup>nd</sup> Edition p. 383, Exercise 1(d))**

*from:* if  $\beta$  is injective,  $\alpha$  and  $\gamma$  are surjective, then  $\gamma$  is injective  
*to:* if  $\beta$  is injective,  $\alpha$  and  $\varphi$  are surjective, then  $\gamma$  is injective

**page 405, Exercise 15 (2<sup>nd</sup> Edition p. 385, Exercise 115)**

*change exercise to:*

Let  $M$  be a left  $\mathbb{Z}$ -module and let  $R$  be a ring with 1.

(a) Show that  $\text{Hom}_{\mathbb{Z}}(R, M)$  is a left  $R$ -module under the action  $(r\varphi)(r') = \varphi(r'r)$  (see Exercise 10).

(b) Suppose that  $0 \rightarrow A \xrightarrow{\psi} B$  is an exact sequence of  $R$ -modules. Prove that if every  $\mathbb{Z}$ -module homomorphism  $f$  from  $A$  to  $M$  lifts to a  $\mathbb{Z}$ -module homomorphism  $F$  from  $B$  to  $M$  with  $f = F \circ \psi$ , then every  $R$ -module homomorphism  $f'$  from  $A$  to  $\text{Hom}_{\mathbb{Z}}(R, M)$  lifts to an  $R$ -module homomorphism  $F'$  from  $B$  to  $\text{Hom}_{\mathbb{Z}}(R, M)$  with  $f' = F' \circ \psi$ . [Given  $f'$ , show

that  $f(a) = f'(a)(1_R)$  defines a  $\mathbb{Z}$ -module homomorphism of  $A$  to  $M$ . If  $F$  is the associated lift of  $f$  to  $B$ , show that  $F'(b)(r) = F(rb)$  defines an  $R$ -module homomorphism from  $B$  to  $\text{Hom}_{\mathbb{Z}}(R, M)$  that lifts  $f'$ .]

(c) Prove that if  $Q$  is an injective  $\mathbb{Z}$ -module then  $\text{Hom}_{\mathbb{Z}}(R, Q)$  is an injective  $R$ -module.

**page 407, last line of Exercise 27(a) (2<sup>nd</sup> Edition p. 387, Exercise 27(a))**

*from:* where  $\pi_1$  and  $\pi_2$  are the natural projections onto

*to:* where  $\pi_1$  and  $\pi_2$  are the restrictions to  $X$  of the natural projections from  $A \oplus B$  onto

**page 423, line 3 of Exercise 9 (2<sup>nd</sup> Edition p. 403, Exercise 9)**

*from:* If  $\varphi|_W$  and  $\tilde{\varphi}$  are

*to:* If  $\varphi|_W$  and  $\tilde{\varphi}$  are

**page 426, line 2 of Exercise 21(b) (2<sup>nd</sup> Edition p. 406, Exercise 21(b))**

*from:*  $6z$

*to:*  $+6z$

**page 433, proof of Theorem 19, line 3**

*from:*  $= E_v(f) + \alpha E_g(v)$

*to:*  $= E_v(f) + \alpha E_v(g)$

**page 435, Exercise 1**

*change exercise to:*

Let  $V$  be a vector space over  $F$  of dimension  $n < \infty$ . Prove that the map  $\varphi \mapsto \varphi^*$  in Theorem 20 is a vector space isomorphism of  $\text{End}(V)$  with  $\text{End}(V^*)$ , but is not a ring homomorphism when  $n > 1$ . Exhibit an  $F$ -algebra isomorphism from  $\text{End}(V)$  to  $\text{End}(V^*)$ .

**page 442, line -8 (2<sup>nd</sup> Edition p. 422, line -8)**

*from:*  $\varphi : M \rightarrow A$  is an  $R$ -algebra

*to:*  $\varphi : M \rightarrow A$  is an  $R$ -module

**page 445, second display in Theorem 34(2) (2<sup>nd</sup> Edition p. 425, Theorem 34(2))**

*from:*  $\iota(m_1, \dots, m_k) = m_1 \otimes \cdots \otimes m_n \text{ mod } \mathcal{C}(M)$

*to:*  $\iota(m_1, \dots, m_k) = m_1 \otimes \cdots \otimes m_k \text{ mod } \mathcal{C}^k(M)$

**page 469, line 1 of Exercise 10 (2<sup>nd</sup> Edition p. 449, Exercise 10)**

*from:*  $N$  an  $R$ -module

*to:*  $N$  a torsion  $R$ -module

**page 479, last sentence of second paragraph (2<sup>nd</sup> Edition p. 459, second paragraph)**

*from:* the degree of the minimal polynomial for  $A$  has degree at most  $n$

*to:* the minimal polynomial for  $A$  has degree at most  $n$

**page 510, line 1 of text (2<sup>nd</sup> Edition p. 490, line 1 of text)**

*from:*  $F$  is a commutative ring with

*to:*  $F$  is a nonzero commutative ring with

**page 555, Exercise 7, bounds for product (2<sup>nd</sup> Edition p. 535, Exercise 7)**

*from:*  $d \mid n$

*to:*  $d \mid m$

**page 566, Example 7, first line after second display**

*from:* we see that  $\sigma_p^{b^n} = 1$

*to:* we see that  $\sigma_p^n = 1$

**page 582, Exercise 17 (2<sup>nd</sup> Edition p. 563, Exercise 17)**

*from:* Let  $K/F$  be any finite extension

*to:* Let  $K/F$  be any finite separable extension

**page 584, Exercise 24 (2<sup>nd</sup> Edition p. 564, Exercise 24)**

*change exercise to:*

Prove that the rational solutions  $a, b \in \mathbb{Q}$  of Pythagoras' equation  $a^2 + b^2 = 1$  are of the form  $a = \frac{s^2 - t^2}{s^2 + t^2}$  and  $b = \frac{2st}{s^2 + t^2}$  for some  $s, t \in \mathbb{Q}$ . Deduce that any right triangle with integer sides has sides of lengths  $((m^2 - n^2)d, 2mnd, (m^2 + n^2)d)$  for some integers  $m, n, d$ . [Note that  $a^2 + b^2 = 1$  is equivalent to  $N_{\mathbb{Q}(i)/\mathbb{Q}}(a + ib) = 1$ , then use Hilbert's Theorem 90 above with  $\beta = s + it$ .]

**page 585, Exercise 29(b) (2<sup>nd</sup> Edition p. 565, Exercise 29(b))**

*from:* Prove that the element  $t =$

*to:* Prove that the element  $s =$

**page 585, Exercise 29(c) (2<sup>nd</sup> Edition p. 565, Exercise 29(c))**

*from:* Prove that  $k(t)$

*to:* Prove that  $k(s)$

**page 617, Exercises (2<sup>nd</sup> Edition p. 598, Exercises)**

The first 10 exercises, excluding Exercise 3, are over the field  $\mathbb{Q}$ .

**page 638, Exercise 18 (2<sup>nd</sup> Edition p. 619, Exercise 18)**

*from:* Let  $D \in \mathbb{Z}$  be a squarefree integer

*to:* Let  $D \neq 1$  be a squarefree integer

**page 654, Exercise 16 (2<sup>nd</sup> Edition p. 635, Exercise 16)**

*from:* Prove that  $F$  does not contain all quadratic extensions of  $\mathbb{Q}$ .

*to:* Prove that  $F$  does contain all quadratic extensions of  $\mathbb{Q}$ . [One way is to consider the polynomials  $x^3 + 3ax + 2a$  for  $a \in \mathbb{Z}^+$ .]

**page 670, line 2 of Exercise 34 (2<sup>nd</sup> Edition p. 648, Exercise 34)**

*from:*  $\text{Ass}_R(N) \subseteq \text{Ass}_R(M)$

*to:*  $\text{Ass}_R(L) \subseteq \text{Ass}_R(M)$

**page 687, Exercise 13 (2<sup>nd</sup> Edition p. 662, Exercise 13)**

*change exercise to:*

Let  $V$  be a nonempty affine algebraic set. Prove that if  $k[V]$  is the direct sum of two nonzero ideals then  $V$  is not connected in the Zariski topology. Prove the converse if  $k$  is algebraically closed. [Use Theorem 31.] Give a counterexample to the converse when  $k$  is not algebraically closed.

**page 707, line 2 of Corollary 37(1) (2<sup>nd</sup> Edition p. 678, Corollary 29(1))**

*from:* if and only if  $D$  contains no zero divisors of  $R$

*to:* if and only if  $D$  contains no zero divisors or zero

**page 713, line 7 of Example 1***from:*  $P_2 \cap \mathbb{Q}[y, z] = (y^5 - z^4)$ *to:*  $P_2 = P \cap \mathbb{Q}[y, z] = (y^5 - z^4)$ **page 721, line 4 after commutative diagram (2<sup>nd</sup> Edition p. 688, line 2)***from:* By Proposition 38(1) [2<sup>nd</sup> Edition: By Proposition 30(1)]*to:* By Proposition 46(1) [2<sup>nd</sup> Edition: By Proposition 36(1)]**page 728, Exercise 21, line 1***from:* Suppose  $\varphi : R \rightarrow S$  is a ring homomorphism*to:* Suppose  $\varphi : R \rightarrow S$  is a ring homomorphism with  $\varphi(1_R) = 1_S$ **page 754, line 2 of Exercise 8 (2<sup>nd</sup> Edition p. 720, Exercise 8)***from:* Observe the*to:* Observe that**page 756, line 1 of proof of Proposition 5 (2<sup>nd</sup> Edition p. 722, proof of Proposition 5)***from:*  $\nu(u) + \nu(v) = \nu(uv) = 1$ *to:*  $\nu(u) + \nu(v) = \nu(uv) = \nu(1) = 0$ **page 761, line 3 of proof of Proposition 10 (2<sup>nd</sup> Edition pp. 727)***from:*  $g : A \rightarrow F$  by  $f(c) =$ *to:*  $g : A \rightarrow F$  by  $g(c) =$ **page 767, line 5 (2<sup>nd</sup> Edition pp. 733)***from:* complete*to:* completes**page 775, lines 1 to 3 of Exercise 24(d) (2<sup>nd</sup> Edition pp. 741–2, Exercise 24(d))***from:*  $P_3 = (3, 1 + \sqrt{-5}) = (3, 5 - \sqrt{-5}) \dots\dots$  [Check that  $\sqrt{-10} = -(5 - \sqrt{-5})\omega/3$ .]*to:*  $P_3 = (3, 1 - \sqrt{-5}) = (3, 5 + \sqrt{-5}) \dots\dots$  [Check that  $\sqrt{-10} = (5 + \sqrt{-5})\omega/3$ .]**page 781, bottom row of diagram (17.9) (2<sup>nd</sup> Edition p. 748, diagram (17.9))***from:*  $0 \rightarrow \text{Hom}_R(A, D) \rightarrow$ *to:*  $0 \rightarrow \text{Hom}_R(A', D) \rightarrow$ **page 793, line 4 of Exercise 11(c) (2<sup>nd</sup> Edition p. 760, Exercise 11(c))***from:* projection maps  $I \rightarrow I_i$ *to:* projection maps  $I \rightarrow I/I_i$ **page 794, Exercise 17 (2<sup>nd</sup> Edition p. 761, Exercise 17)***from:* for any abelian group  $A$ *to:* for any abelian group  $B$ **page 800, line –7 (2<sup>nd</sup> Edition p. 766, line –7)***from:*  $H^n(G, A) \cong \text{Ext}^n(\mathbb{Z}, A)$ *to:*  $H^n(G, A) \cong \text{Ext}_{\mathbb{Z}G}^n(\mathbb{Z}, A)$

**page 801, line 4 (2<sup>nd</sup> Edition p. 767, line 4)**

*from:* 1 if  $n$  is odd  
*to:*  $a$  if  $n$  is odd

**page 812, Exercise 18(a) (2<sup>nd</sup> Edition p. 778, Exercise 18(a))**

*from:* from  $\mathbb{Z}/(m/d)\mathbb{Z}$  to  $\mathbb{Z}/m\mathbb{Z}$  if  $n$  is odd, and from 0 to 0 if  $n$  is even,  $n \geq 2$ ,  
*to:* from 0 to 0 if  $n$  is odd, and from  $\mathbb{Z}/(m/d)\mathbb{Z}$  to  $\mathbb{Z}/m\mathbb{Z}$  if  $n$  is even,  $n \geq 2$ ,

**page 813, line 3 of Exercise 19 (2<sup>nd</sup> Edition p. 779, Exercise 19)**

*from:*  $p$ -primary component of  $H^1(G, A)$   
*to:*  $p$ -primary component of  $H^n(G, A)$

**page 815, line 2 of Proposition 30 (2<sup>nd</sup> Edition p. 781)**

*from:* group homomorphisms from  $G$  to  $H$   
*to:* group homomorphisms from  $G$  to  $A$

**page 816, line -13 (2<sup>nd</sup> Edition p. 782, line -13)**

*from:* bijection between the elements of  
*to:* bijection between the cyclic subgroups of order dividing  $n$  of

**page 823, Exercise 9(b) (2<sup>nd</sup> Edition p. 789, Exercise 9(b))**

*from:*  $H^1(A_n, V) = 0$  for all  $p$   
*to:*  $|H^1(A_n, V)| = \begin{cases} 3, & \text{if } p = 3 \text{ with } n = 4 \text{ or } 5 \\ 0, & \text{otherwise} \end{cases}$

**page 832, lines -10 and -14 (2<sup>nd</sup> Edition p. 798, lines -6 and -10)**

*from:*  $L$   
*to:*  $K$

**page 853, line 4 of Exercise 17 (2<sup>nd</sup> Edition p. 819, Exercise 17)**

*from:* Your proof ...  
*to:* Your proof that  $\varphi$  has degree 1 should also work for infinite abelian groups when  $\varphi$  has finite degree.

**page 869, line -6 (2<sup>nd</sup> Edition p. 835, line -6)**

*from:* the isotypic components of  $G$   
*to:* the isotypic components of  $M$

**page 885, Exercise 8 (2<sup>nd</sup> Edition p. 851, Exercise 8)**

*from:* This table contains nonreal entries.  
*to:* This table contains irrational entries.

**page 893, line 4 (2<sup>nd</sup> Edition p. 859, line 4)**

*from:* a proper, nontrivial subgroup of  $G$   
*to:* a proper, nontrivial normal subgroup of  $G$

**page 897, line 7 (2<sup>nd</sup> Edition p. 863)**

*Replace from "Let  $\psi \dots$ " to end of proof with:*

Let  $\mathcal{C}$  be the set of nonprincipal irreducible characters of  $Q$ . For each  $\psi \in \mathcal{C}$  and each  $i = 0, 1, \dots, p-1$  define

$$\psi_i(h) = \psi(x^i h x^{-i}) \quad \text{for all } h \in Q.$$

Since  $\psi_i$  is a homomorphism from  $Q$  into  $\mathbb{C}^\times$  it is also an irreducible character of  $Q$ . Thus  $P = \langle x \rangle$  permutes  $\mathcal{C}$  via the (right) action  $\psi^{x^i} = \psi_i$  (see Exercise 10).

If  $\psi_i = \psi_j$  for some  $i > j$  then  $\psi(x^i h x^{-i}) = \psi(x^j h x^{-j})$  and so  $\psi(h) = \psi(x^{i-j} h x^{j-i})$  for all  $h \in Q$ . Let  $k = i - j$  so that  $\psi = \psi_k$ . Thus  $\ker \psi = \ker \psi_k$  and it follows that  $x^k$  normalizes  $\ker \psi$ . Since  $\langle x \rangle = \langle x^k \rangle$  acts irreducibly on  $Q$ ,  $\ker \psi = 1$ . Thus  $\psi$  is a faithful character. But  $G$  is a Frobenius group so  $h \neq x^k h x^{-k}$  for every nonidentity  $h \in Q$ , contrary to  $\psi(h) = \psi(x^k h x^{-k})$ . This proves  $\psi_0, \dots, \psi_{p-1}$  are distinct irreducible characters of  $Q$ , i.e.,  $P$  acts without fixed points on  $\mathcal{C}$ .

Next let  $\psi \in \mathcal{C}$  and let  $\Psi = \text{Ind}_Q^G(\psi)$ . We use the orthogonality relations and the preceding results to show that  $\Psi$  is irreducible. Since  $1, x^{-1}, \dots, x^{-(p-1)}$  are coset representatives for  $Q$  in  $G$  and, by Corollary 12,  $\Psi$  is zero on  $G - Q$  we have

$$\begin{aligned} \|\Psi\|^2 &= \frac{1}{|G|} \sum_{h \in Q} \Psi(h) \overline{\Psi(h)} \\ &= \frac{1}{|G|} \sum_{h \in Q} \sum_{i=0}^{p-1} \psi(x^i h x^{-i}) \sum_{j=0}^{p-1} \overline{\psi(x^j h x^{-j})} \\ &= \frac{1}{|G|} \sum_{i,j=0}^{p-1} \sum_{h \in Q} \psi_i(h) \overline{\psi_j(h)} \\ &= \frac{1}{|G|} |Q| \sum_{i,j=0}^{p-1} (\psi_i, \psi_j)_Q = \frac{1}{|G|} |Q| p = 1 \end{aligned}$$

where the second line follows from the definition of the induced character  $\Psi$ , and the last line follows because the previous paragraph gives  $(\psi_i, \psi_j)_Q = \delta_{ij}$ . This proves  $\Psi$  is an irreducible character of  $G$ .

Finally we show that every irreducible character of  $G$  of degree  $> 1$  is induced from some nonprincipal degree 1 character of  $Q$  by counting the number of distinct irreducible characters of  $G$  obtained this way. By parts (1) and (2) the number of irreducible characters of  $G$  (= the number of conjugacy classes) is  $p + (q^a - 1)/p$  and the number of degree 1 characters is  $p$ . Thus the number of irreducible characters of  $G$  of degree  $> 1$  is  $(q^a - 1)/p$ . Each  $\psi \in \mathcal{C}$  induces to an irreducible character of degree  $p$  of  $G$ . Characters  $\psi_i, \psi_j$  in the same orbit of  $P$  acting on  $\mathcal{C}$  induce to the same character of  $G$  (which is zero outside  $Q$  and on  $Q$  it is  $\sum_{i=0}^{p-1} \psi_i$ ). One easily computes that characters in different orbits of  $P$  on  $\mathcal{C}$  induce to orthogonal irreducible characters of  $G$ . Since  $P$  acts without fixed points on  $\mathcal{C}$ , the number of its orbits is  $|\mathcal{C}|/p = (q^a - 1)/p$ . This accounts for all irreducible characters of  $G$  of degree  $> 1$ , and all such have degree  $p$ . The proof is complete.

**page 899, line 1 of item (3) (2<sup>nd</sup> Edition p. 865)**

*from:* let  $Q_3$  be a Sylow 11-subgroup of  $G$

*to:* let  $Q_3$  be a Sylow 13-subgroup of  $G$

**page 907, Exercise 1(a) (2<sup>nd</sup> Edition p. 873, Exercise 1(a))**

*from:* a 3-tuple in  $A \times A \times A$  maps to an ordered pair in  $A \times A$

*to:* an ordered pair in  $A \times A$  maps to a 3-tuple in  $A \times A \times A$

**page 912, line 6 (2<sup>nd</sup> Edition p. 878, line 6)**

*from:* if  $A \neq B$  or  $C \neq D$

*to:* if  $A \neq C$  or  $B \neq D$